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# Spatial uniformity of the spectral radiance by white LED-based K<sub>2</sub>CaP<sub>2</sub>O<sub>7</sub>:Ce<sup>3+</sup>, Tb<sup>3+</sup> phosphor

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## **ABSTRACT**

The K<sub>2</sub>CaP<sub>2</sub>O<sub>7</sub>:Ce<sup>3+</sup>, Tb<sup>3+</sup> (Ce/Tb-KCPO) phosphor with blue-to-green emission is introduced in this study. The synthesis of the phosphor is carried out with the solid-state approach. The phosphor characteristics, including X-ray diffraction, luminescence lifespan, and thermal stability are measured and examined. The data show that Ce/Tb-KCPO phosphor displays a broadband emission from blue to green when excited by ultraviolet source. Besides, the ion Ce<sup>3+</sup> strengthen the emission of Tb<sup>3+</sup> ion through an efficient energy-transfer mechanism, which is estimated about 82.51%. The main electric interaction responsible for this Ce/Tb energy transfer is the dipole-quadrupole one. The phosphor also benefits the luminous intensity and color uniformity of the light-emitting diodes (LED) white-light output. Therefore, the Ce/Tb-KCPO phosphor can be a potential material for highpower white light-emitting diodes (WLED).

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## INTRODUCTION

With exceptional properties like great brightness, long-term service, ease of manufacture, and low toxicity, inorganic luminescence compounds have been the topic of many researchers' interest [1], [2]. One of the most promising materials is the rare-earth-based compounds [3]. The rare earth ions have a unique 4F shell arrangement, allowing them to be able to produce good hues. By mixing various rare earth ions and adjusting the ion dopant's ratio, it is possible to obtain distinguish excitation energies and nearly the whole visible light spectrum from violet to red. In terms of green spectral wavelength, the ion Tb<sup>3+</sup> is a typical activator for its strong emission centered at roughly 545 nm, owing to the transition of  ${}^5D_4 \rightarrow {}^7F_5$  [4]-[6]. Nevertheless, using only Tb<sup>3+</sup> ion in a phosphor host is insufficient for practical uses owing to its inferior absorption lines of 4F-4F spin-forbidden transitions [7]. However, the emission strength of Tb<sup>3+</sup> can be heightened using a suitable sensitizer, especially Ce<sup>3+</sup> ions. Meanwhile, depending on the nature of the base materials, the co-doped phosphor typically shows an absorption band of f-d for Ce3+, which extends from ultraviolet to visible light, making it possible to greatly widen Tb<sup>3+</sup> applications [8].

The host lattice for doping Ce<sup>3+</sup> and Tb<sup>3+</sup> also has an imperative effect on the phosphor material's performance. Among the host materials, pyrophosphate has been demonstrated a broadband gap and high-efficiency material, which also offers excellent thermal and chemical stability [9], [10]. It was reported that the phosphor with pyrophosphate host could be synthesized at a lower heat (not exceeding 800 °C) than other base such as aluminates or silicates (>1,200 °C). In the pyrophosphate variations, K<sub>2</sub>CaP<sub>2</sub>O<sub>7</sub> (KCPO) contains enough substitutable space for the rare earth ions. Given the benefits listed above, KCPO could be

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an excellent host lattice for luminous compounds. However, there has been limited study on KCPO hosts and on Ce<sup>3+</sup>/Tb<sup>3+</sup>-co-activated KCPO material [11], [12].

In this research, we center on the development of a KCPO-based phosphor with small amount of energy consumption and great thermal stability. In addition, the investigation of the luminous performance of Ce<sup>3+</sup> and Tb<sup>3+</sup> in the KCPO host is also demonstrated. The phosphor was produced using the solid-state technique. To validate the phosphors' purity and the influence of the dopants' amount on crystal geometry, the crystal phase and site replacement were explored. To understand the luminous mechanism of the ion dopants as well as the power shift process among Ce<sup>3+</sup> and Tb<sup>3+</sup> within the KCPO base, the luminous performance including excitation, emission spectra, along with the chromaticity diagram was reviewed. Furthermore, thermal stability was investigated in order to investigate potential effectiveness.

## 2. METHOD

# **2.1.** Creating K<sub>2</sub>CaP<sub>2</sub>O<sub>7</sub>:Ce<sup>3+</sup>, Tb<sup>3+</sup> (Ce/Tb-KCPO)

The phosphor with blue-green phosphor Ce/Tb-KCPO was synthesized utilizing the solid-state technique. The chemical elements of the phosphor composition and synthesizing process of the phosphor were presented in Table 1 [13]. The employed elements are uncomtaminated.

Table 1. Raw ingredients and synthesizing process of Ce/Tb-KCPO phosphor

|  | Materials                      | Purity (%) | Synthesizing procedure   |
|--|--------------------------------|------------|--|
|  | K <sub>2</sub> CO <sub>3</sub> | 99.99      | 1. The uncomtaminated ingredients were weighed stoichiometrically and well mixed in a mortar.  |
|  | CaCO <sub>3</sub>              | 99.99      | 2. The mixture was ground thoroughly.  |
|  | $NH_4H_2PO_4$                  | 99.99      | 3. The ground sample was calcined in an alumina crucible at ~780 °C for four hours, with 5 vol |
|  | $CeO_2$                        | 99.99      | % H <sub>2</sub> in N <sub>2</sub> .   |
|  | $Tb_4O_7$                      | 99.99      | 4. The phosphor sample was cooled down to room temperature and re-ground.                      |

## 2.2. Phosphor characteristics and measuring instruments

Table 2 shows the characteristics of the prepared phosphor that were examined and the corresponding determing instruments [14]. Besides, the phosphor was applied to create a white light-emitting diodes (WLED) model for further investigations. Figure 1 shows the components and the structure of the required WLED package. Figure 1(a) is the true photograph of the WLED model; Figures 1(b) and (c) display the diagram of bonding light-emitting diodes (LED) chip and the phosphor-layer organization in the model; Figure 1(d) shows the WLED 3D simulation built by the LightTools software [15], [16]. Here, the influences of the Ce/Tb-KCPO is examined with the variation of its concentration (wt %), and the results will be discussed in the next section.

Table 2. Characteristics of the phosphor and corresponding measuring instruments

| Characteristics                            | Instruments  |
|--|--|
| Patterns of X-ray diffraction (XRD)        | Bruker D8 advance, with 2θ range of 10-60°, a radiation Cu-Kα (~0.15405 nm), at    |
|  | 30 kV and 40 mA.   |
| Emission spectrum and excitation           | Hitachi F-4500 fluorescence spectrophotometer, with excitation source of a Xe lamp |
| spectrum                                   | (150 W).   |
| Luminescent lifetime and thermal stability | HORIBA Jobin Yvon Fluorolog-3.   |

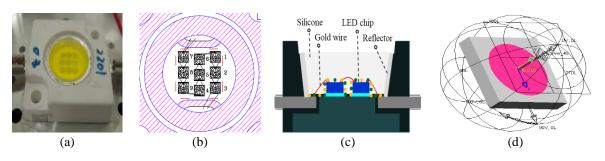


Figure 1. Pictures depicting WLED formation (a) WLED device, (b) binding graph, (c) pc-WLED illustrated, and (d) recreating WLED device via program LightTools

#### 3. RESULTS AND DISCUSSION

#### 3.1. Computation

The energy transfer process of the doped ions in the host can affect the emission performance of the phosphor. This feature of the Ce/Tb-KCPO phosphor can be mathematically determined by estimating the critical distance Rc among the ions of Tb<sup>3+</sup> and Ce<sup>3+</sup>. The Rc could be determined through the expression of concentration quenching in (1) [17]:

$$Rc \approx 2 \times [(3V)/(4\pi X cN)]^{1/3} \tag{1}$$

Where V, Xc, and N represent the unit-cell volume, the sum optimal concentration of  $Tb^{3+}$  and  $Ce^{3+}$ , and the center cation's number in the crystal, respectively. For the KCPO host, we get the values of V, Xc, and N of 700.94 Å<sup>3</sup>, 0.14, and 4, respectively. As a result, the obtained Rc is about 13.37 Å, which greatly exceeds 5 Å. Therefore, the  $Ce^{3+}/Tb^3$  ion power shift process in the host would be attributed to the electric multipolar interaction. Then, the multipolar-interaction kind can be determined with Dexter-theory in (2):

$$\frac{\eta_0}{\eta} \infty C^{n/3} \tag{2}$$

Where n can be 6, 8, and 10. With n=6, the interaction is dipole-dipole, while n=8 is dipole-quadrupole and n=10 is quadrupole-quadrupole.  $\eta$  and  $\eta_0$  represent the Ce<sup>3+</sup> luminous quantum efficacy in the Tb<sup>3+</sup> presence and absence, respectively. C indicates the activators' concentration. Based on the approximation of Reisfeld,  $\frac{\eta_0}{\eta}$  can be altered by the related-luminescence intensities' ratio ( $\frac{I_{SO}}{I_S}$ ), as expressed in (3) [18]:

$$\frac{I_{SO}}{I_S} \infty C^{n/3} \tag{3}$$

Where  $I_{SO}$  is the luminescent strength of the KCPO:xCe<sup>3+</sup> (x=0.02), and  $I_S$  is the luminescent strength of xCe/yTb-KCPO (x=0.02; y=0-0.2). In regard to the  $\frac{I_{SO}}{I_S}$  dependence on C<sup>6/3</sup>, C<sup>8/3</sup>, and C<sup>10/3</sup> for Ce<sup>3+</sup> emission, the linear connection could be recorded as n=8, which means the dipole-quadrupole interactivity would be the most significant for the Ce<sup>3+</sup>/Tb<sup>3+</sup> power shift within the KPCO base. The temperature-dependent luminescent strength (S<sub>T</sub>) and the activation power (P<sub>a</sub>) can be clarified and using (4) [19]:

$$S_T = \frac{S_0}{1 + c \exp[P_a/(-kT)]} \tag{4}$$

where  $S_T$  and  $S_0$  represent the luminescent strength of  $Tb^{3+}$  at the temperatures of different measurements and at room temperature, respectively, c signifies a constant, k signifies Boltzmann constant.

# 3.2. Phosphor influence on white light-emitting diodes

When the phosphor Ce/Tb-KCPO is used in the WLED model, the concentration of the phosphor has significant effects on the lighting properties of the WLED. The scattering of the forward scattering of the light seems to be enhanced with the presence of this blue-green emission phosphor. Figure 2 displays the reduced scattering coefficients (RSC) of the WLED with increasing concentration of Ce/Tb-KCPo phosphor. The figure presents that the increasing phosphor concentration leads to the increase in the RSC, meaning that the backward scattering is possibly reduces, allowing more light to transmit through the phosphor layer and escape from the LED [20]. As a result, the light output intensity can be enhanced.

Besides, the addition of Ce/Tb-KCPO cause the YAG:Ce yellow-phosphor concentration to decreases to serve the purpose of stabilizing correlated color temperature (CCT). This phenomenon is displayed by Figure 3. The higher the concentration for Ce/Tb-KCPO, the lower the YAG:Ce concentration. Moreover, the decrease of YAG:Ce content helps increase the forward scattering and enhance the color uniformity of the generated white light.

Figures 4 and 5 help clarify the benefits of Ce/Tb-KCPO improving the hue uniformity for the WLED light output. Particularly, Figure 4 shows the CCT values for the WLED with different concentration of Ce/Tb-KCPO, while Figure 5 shows the decline in CCT deviation (D-CCT, color deviation) [21]. Obviously, the increasing of the blue-green phosphor (0–25%) can keep the variation of CCT to the lower level. 25% Ce/Tb-KCPO shows the lowest CCT deviation (Figure 5), indicating that the color uniformity with 25% concentration of this phosphor is the highest.

Besides the color uniformity, the color rendition ability of the white-light is important. The rendition ability of the white light with increasing concentration of Ce/Tb-KCPO phosphor can be validated via the color rendering index (CRI) along with color quality scale (CQS), which will be shown in Figures 6 and 7,

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respectively. As illustrated, heightened concentration values of the phosphor decrease the CRI and CQS [22]–[24]. The color rendition can be enhanced with wide-band emission that can cover the orange-red region. However, the emission of the Ce/Tb-KCPO is strong between the blue and green regions and weak in the orange-red band. Consequently, the red component is not enough to give good combination for the improved CRI and CQS. Additionally, the strong absorption of the Ce/Tb-KCPO is partially attributed to the declining CQS and CRI. Particularly, the phosphor granules strongly absorbed the blue illumination generated by LED chip as well as the yellow illumination generated by the phosphor YAG:Ce, which allows the phosphor to convert these lights to generate more green lights. Hence, the green light components are much greater than the others, making the light inefficiently rendering the color as expected.

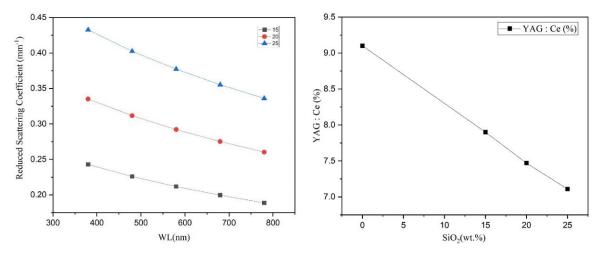


Figure 2. RSC with increasing Ce/Tb-KCPO content

Figure 3. YAG:Ce weight percentage reducing with increasing Ce/Tb-KCPO concentration

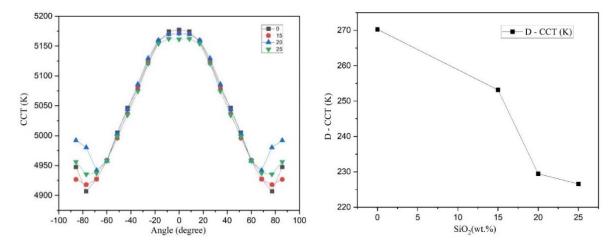
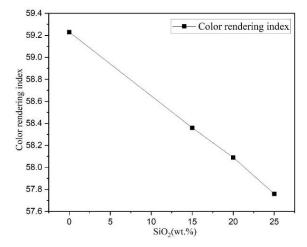


Figure 4. WLED's CCT values change with the concentration of the Ce/Tb-KCPO phosphor

Figure 5. WLED's CCT deviation along with Ce/Tb-KCPO concentration

The luminous of the WLED with Ce/Tb-KCPO is also a critical category to assess. Figure 8 shows the rise in luminosity of the WLED if the concentration for the Ce/Tb-KCPO phosphor increase from 0% to 25%. This means the total light escaping from the LED dome is enhanced. It is possibly ascribed to the enhanced forward scattering and stronger blue-green emission. Figure 9 displays the total emission power of the WLED with Ce/Tb-KCPO phosphor (0–25%), from which the stimulated blue-green emission regions can be clarified. The figure depicts the two peaks of the WLED emission in the blue region at ~450 nm and green region at ~545 nm. So, the Ce/Tb-KCPO phosphor can be useful in obtaining greater luminosity along with enhanced color uniformity for WLED light [25].

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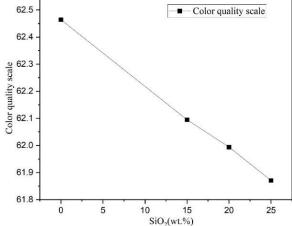
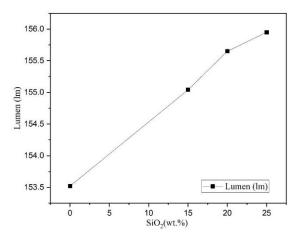


Figure 6. WLED's color rendering index with different Ce/Tb-KCPO concentrations

Figure 7. WLED's color quality scale with Ce/Tb-KCPO phosphor presence



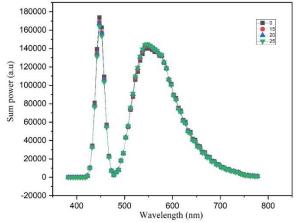


Figure 8. WLED's lumen with different Ce/Tb-KCPO concentrations

Figure 9. WLED's emission power with Ce/Tb-KCPO phosphor presence

# 4. CONCLUSION

This study demonstrated the Ce/Tb-KCPO phosphor with blue-green emission, which can be prepared using solid-state synthesizing method. The optimal luminescence of the phosphor can be obtained by modifying the concentration of the ion dopants. The phosphor shows blue-green emission color as a result of the energy-transferring influence of Ce<sup>3+</sup>→Tb<sup>3+</sup>. The energy transfer strength varies with the increasing content of the Tb<sup>3+</sup> ion dopant in the phosphor composition. The electric interaction of dipole-quadrupole is observed to be responsible for the power shift process among the activated ions within the KCPO host. Besides, the phosphor exhibits good thermal stability with the temperature range of 77–673 K. The phosphor also demonstrates its advantage in stimulating the luminescent intensity and uniform color properties of the white light from the as-prepared WLED model. The color rendition performance, on the other hand, steadily decreases as the phosphor content increase, according to the decline of both CRI and CQS values. Thus, the Ce/Tb-KCPO phosphor have potential in solid-state lighting technology and high-power LED devices.

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